AUT Admission Sample Question

1. Let $f(x) = x^2 - 2x + a$. The graph of f(x) meets the graph of y = 0 at only one point. Find a.

- 1 -1 2 0 3 1 4 2 5 3
- 2. When $\mathbf{z} = \frac{1+\mathbf{i}}{\sqrt{2}}$, find \mathbf{z}^3 .
- ①1 ② i ③ -i ④ $\frac{1+i}{\sqrt{2}}$ ⑤ $\frac{-1+i}{\sqrt{2}}$
- 3. Simplify the following:

$$\lim_{x \to \infty} \left(\frac{3^{x} + 5^{x+1}}{2^{x} - 5^{x-1}} \right)$$

- (1)-63 (2) -25 (3) $\frac{8}{3}$ (4) $-\frac{8}{3}$ (5) 1
- 4. Find the minimum value of $x^2 4x + 8$.
- 1) 2 2 4 3) 6 4) 8 5) 10
- 5. Let $A = \begin{pmatrix} 2 & a \\ 0 & 1 \end{pmatrix}$ and if $A^2 = \begin{pmatrix} b & 3 \\ c & d \end{pmatrix}$, what is a + b + c + d?

 1) 2 2 3 3 4 4 5 5 6

6. Jeff bought a used car for \$4000 and paid 20% deposit. How much does he still have to pay?

- ① \$800 ② \$2000 ③ \$2500 **④** \$3200 ⑤ None of these
- 7. Evaluate $\int_{5}^{6} (x-5)^4 x \, dx$.
- (1) $1\frac{1}{6}$ (2) $1\frac{1}{7}$ (3) $1\frac{1}{8}$ (4) $1\frac{1}{9}$ (5) None of these

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8. When $2^a=3^b=8$ and $\frac{a}{b}=log_2c$, find c.

- 1) 2 2 3 3 4 4 5 5 6

9. Evaluate $\lim_{x\to 0} \left(\frac{\cos 3x-1}{x^2}\right)$

- ① $\frac{9}{2}$ ② $\frac{3}{2}$ ③ $-\frac{2}{3}$ ④ $-\frac{9}{2}$ ⑤ None of these

10. When $a - \frac{1}{a} = 2$, find $a + \frac{1}{a}$.

- 1 $2\sqrt{2}$ 2 $\sqrt{3}$ 3 $-2\sqrt{5}$ 4 $-\sqrt{2}$ 5 $2\sqrt{5}$